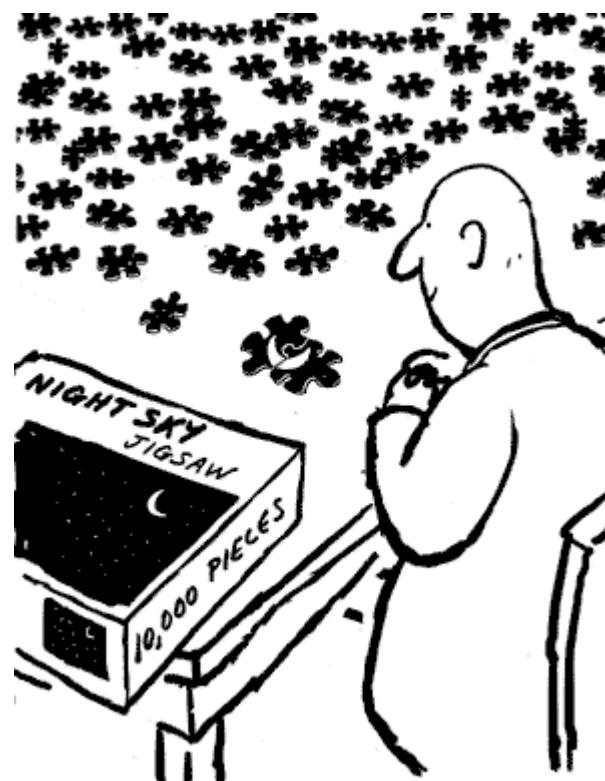


# **AS750 Observational Astronomy**

Prof. Sebastian Lopez  
Lecture 8

# Observational limitations



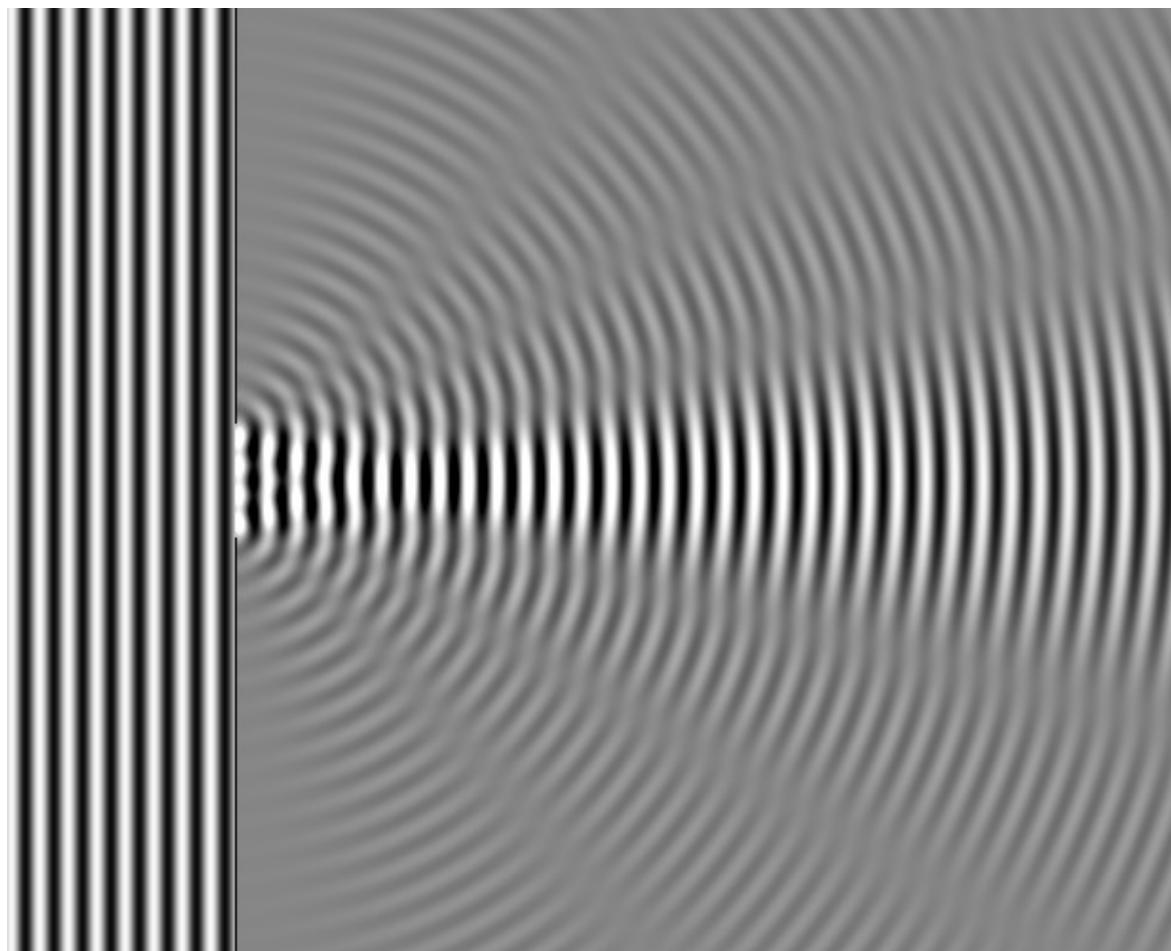
# Observational limitations

- 0) Poisson! (quantum limitation)
- 1) Diffraction limit
- 2) Detection (aperture) limit
  - a) Simple case
  - b) More realistic case
- 3) Atmosphere



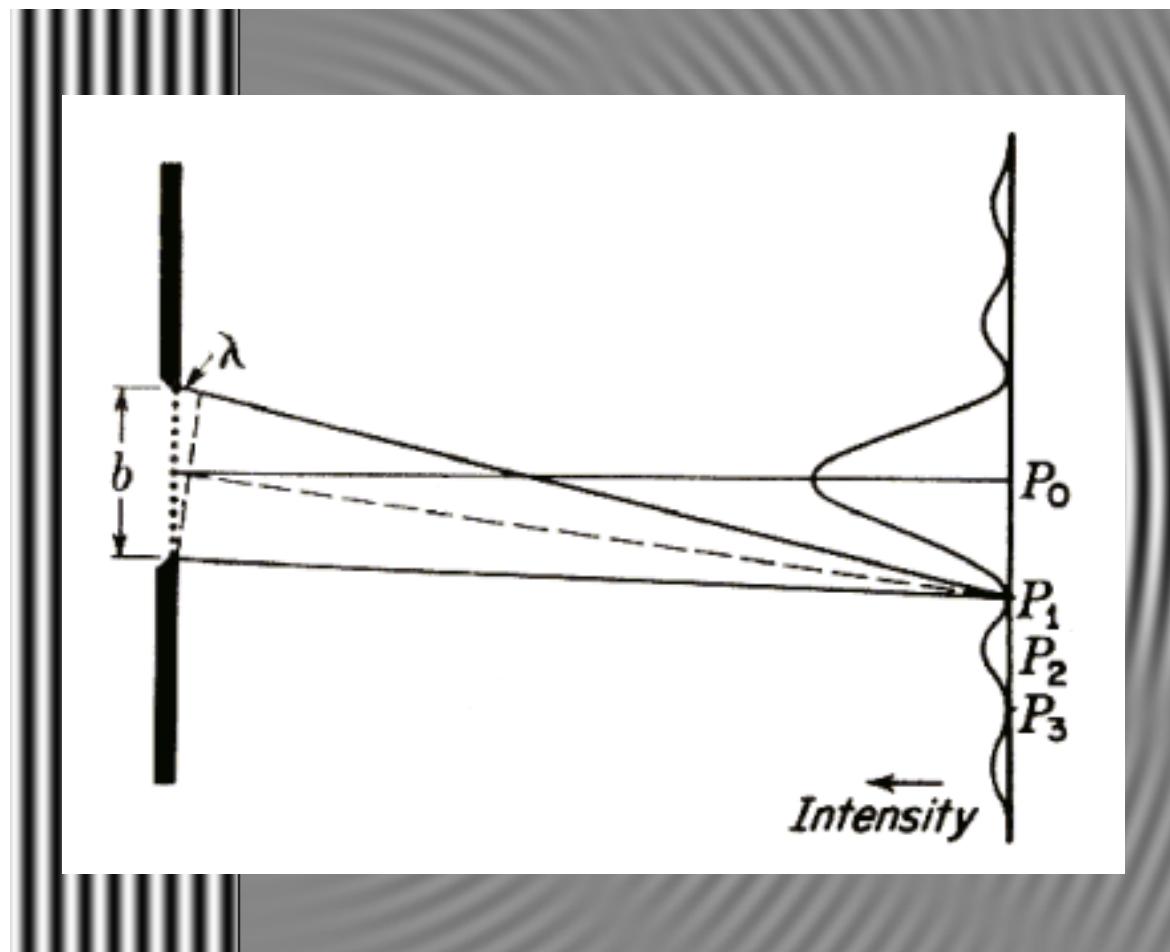
# Observational limitations

## 1) Diffraction limit



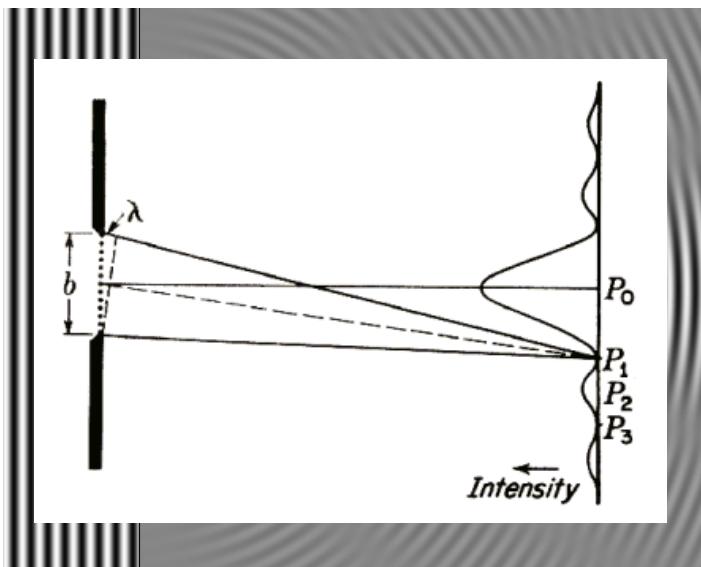
# Observational limitations

Diffraction limit: if the source is coherent the diffraction pattern is produced by constructive and destructive superposition.



# Observational limitations

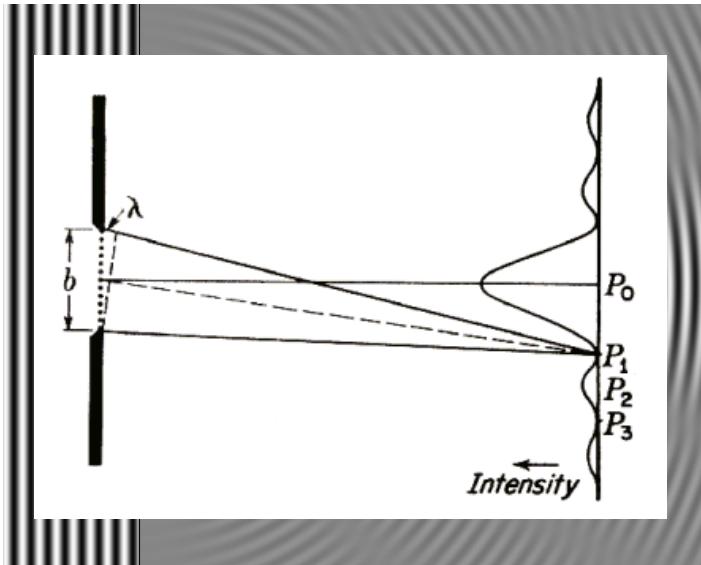
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Phase:  $\phi = \frac{2\pi}{\lambda} b \sin \theta$

# Observational limitations

Diffraction limit: if the source is coherent the diffraction pattern is produced by constructive and destructive superposition.



$$\text{Phase: } \phi = \frac{2\pi}{\lambda} b \sin \theta$$

Distribution of intensities is given by the power Spectrum of the Fourier Transform of the pattern:

$$I_\theta = I_0 \frac{\sin^2(\pi b \sin \theta / \lambda)}{\left(\frac{\pi}{\lambda} \sin \theta\right)^2}$$

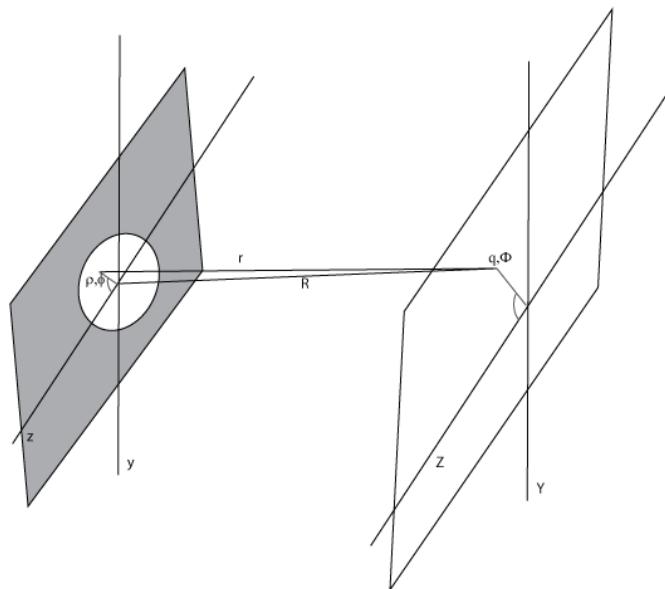
Two parallel slits separated by a distance  $d$

# Observational limitations

For a circular aperture:

$$I_\theta \propto \frac{\pi^2 r^4}{m^2} (J_1(2m))^2$$

Where: J is a Bessel function, r the radio of the aperture and:

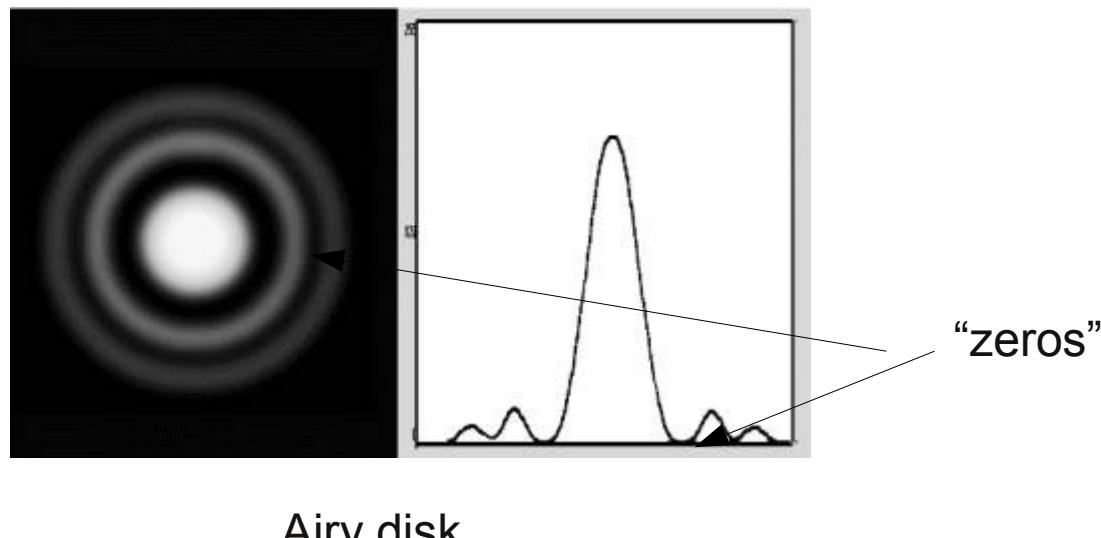


$$m = \frac{\pi r \sin \theta}{\lambda}$$

(see Kitchin, Chapt 1)

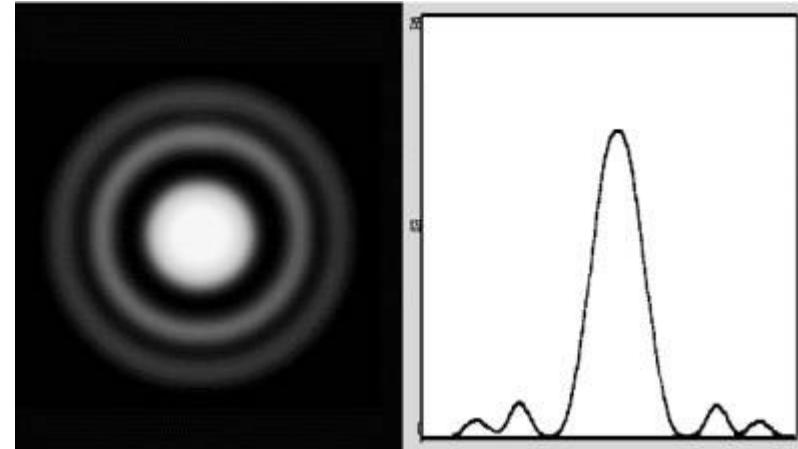
# Observational limitations

For a circular aperture:



# Observational limitations

For a circular aperture:



$$m = 1.916, 3.508, \dots$$

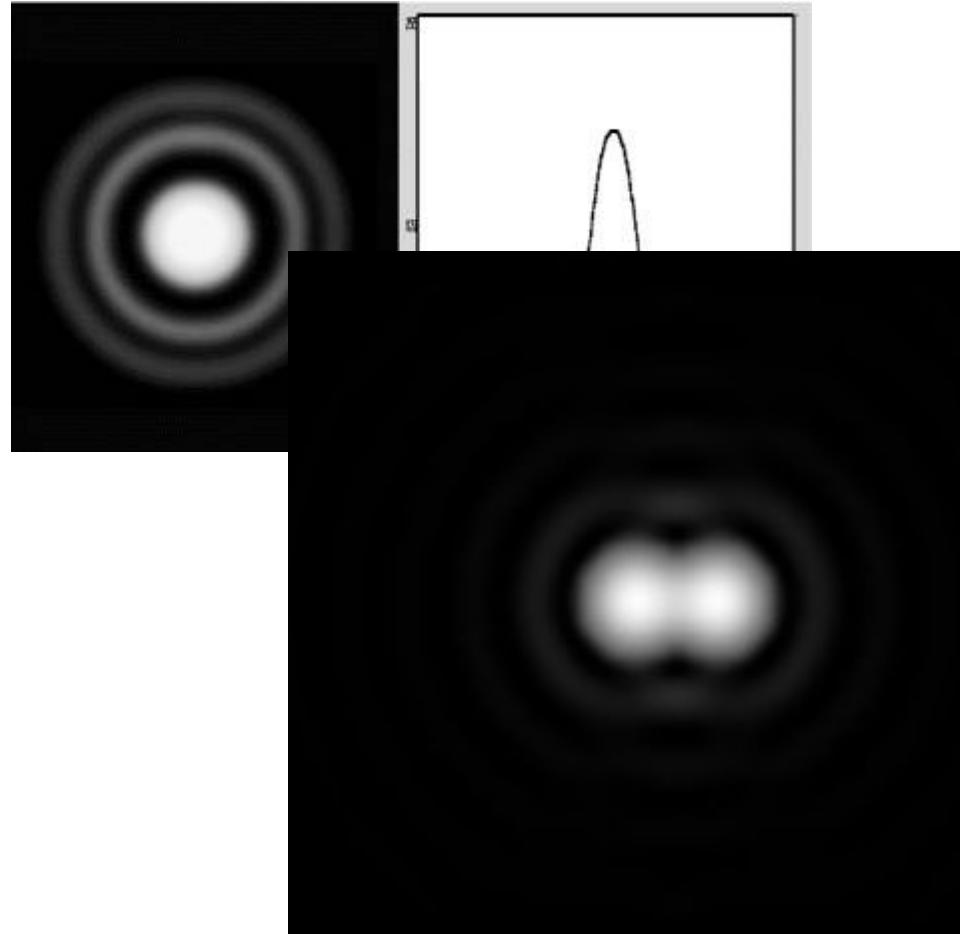
$$\sin \theta = \frac{1.916}{\pi r} \lambda, \frac{3.508}{\pi r} \lambda, \dots$$

$d=2r$

$$\theta \approx \frac{1.220}{d} \lambda, \frac{2.233}{d} \lambda, \dots$$

# Observational limitations

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$$m = 1.916, 3.508, \dots$$

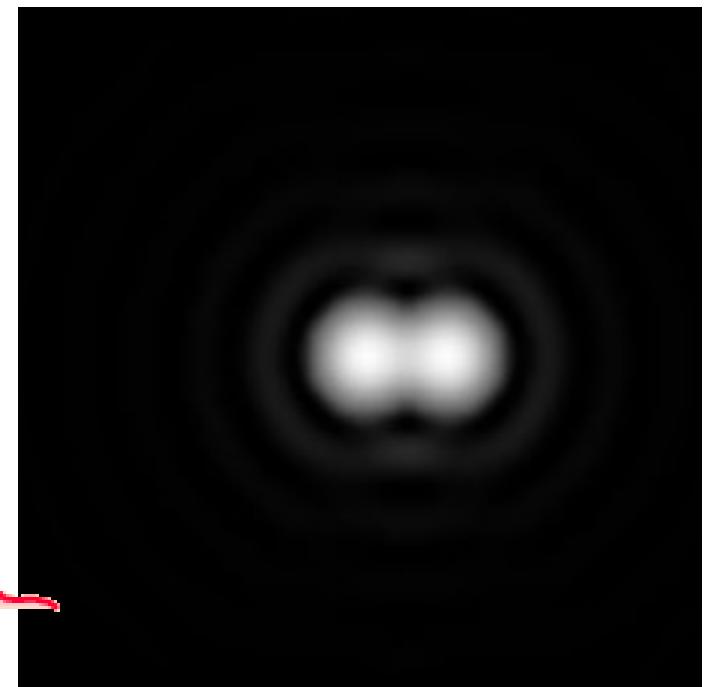
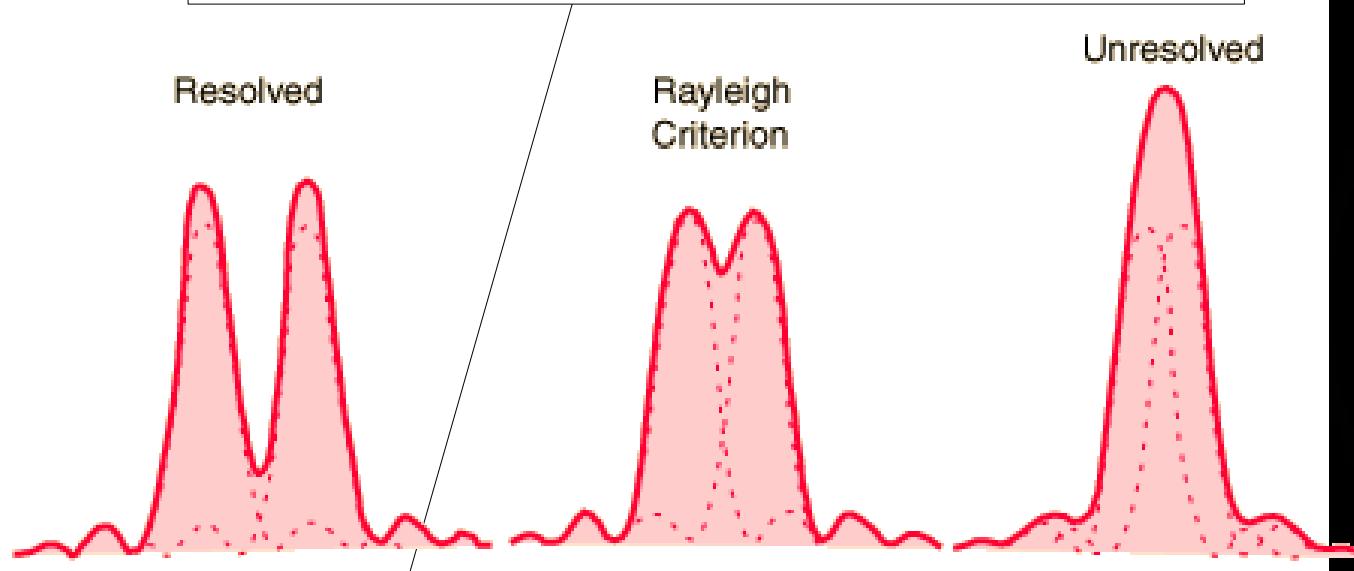
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Rayleigh's criterion for resolving two sources.

# Observational limitations

Rayleigh's criterion for resolving two sources  
(circular aperture).



$$\theta \approx \frac{1.220}{d} \lambda$$

# Observational limitations

Examples:

- Human pupil:  $d=8$  mm, @ 5000 Å,  $\alpha = 15$  arcsec

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- Gemini telescope:  $d= 8$  m, @ 10.,000 Å,  $\alpha = 0.03$  arcsec

# Observational limitations

Examples:

- Human pupil:
- Hubble Space
- Gemini telesco



# Observational limitations

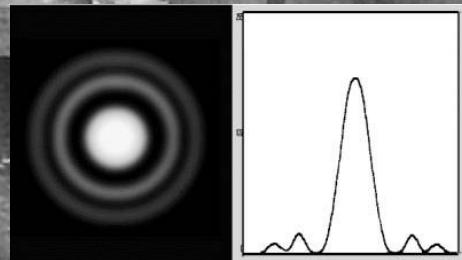
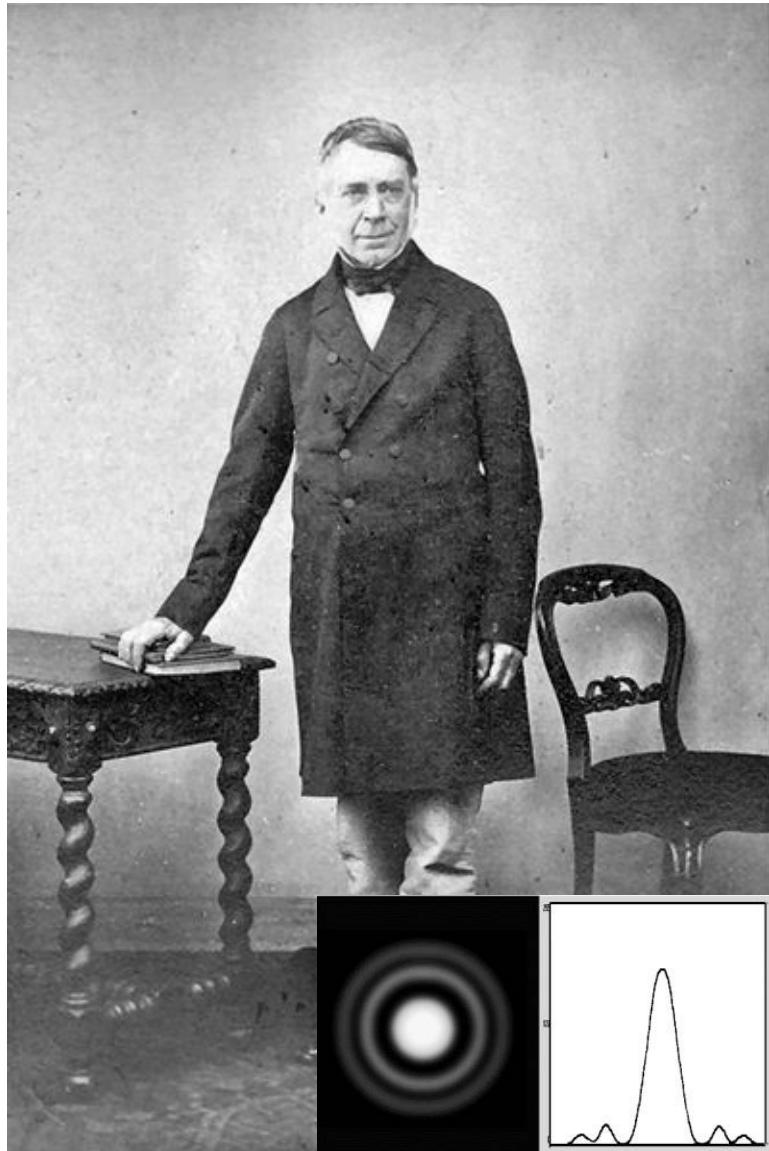
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Eye receptors ~ 1 arcmin

Atmospheric seeing ~0.5 arcsec

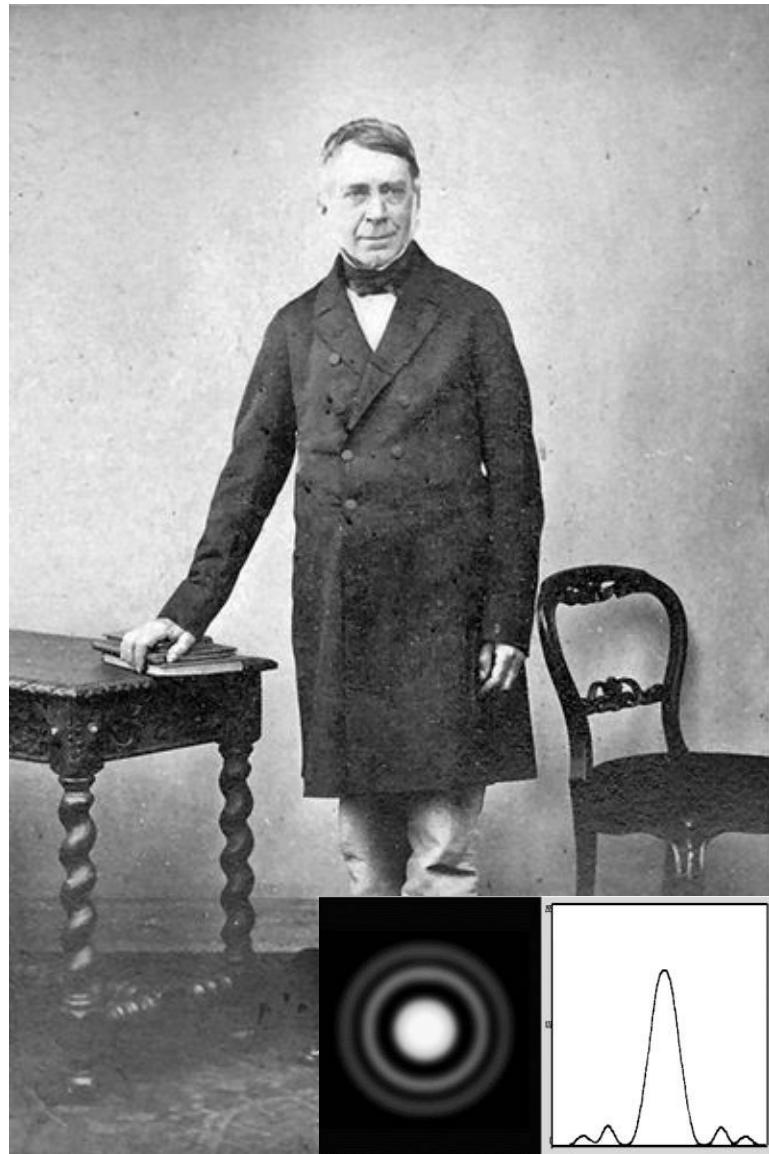
# Observational limitations



George Airy

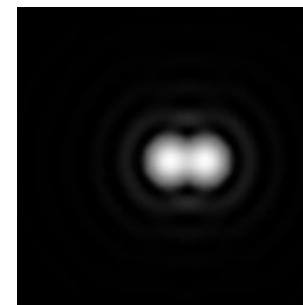
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# Observational limitations



George Airy

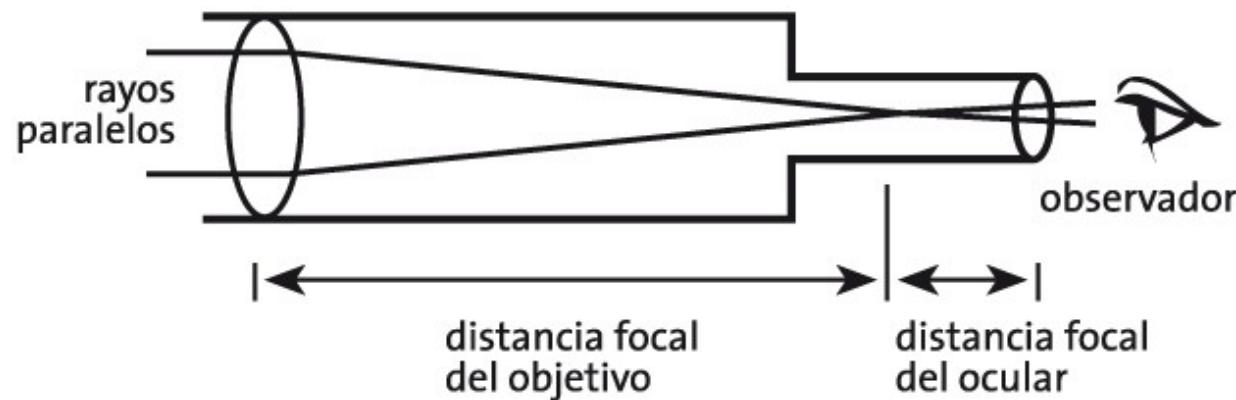
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John Strutt  
(Lord Rayleigh)

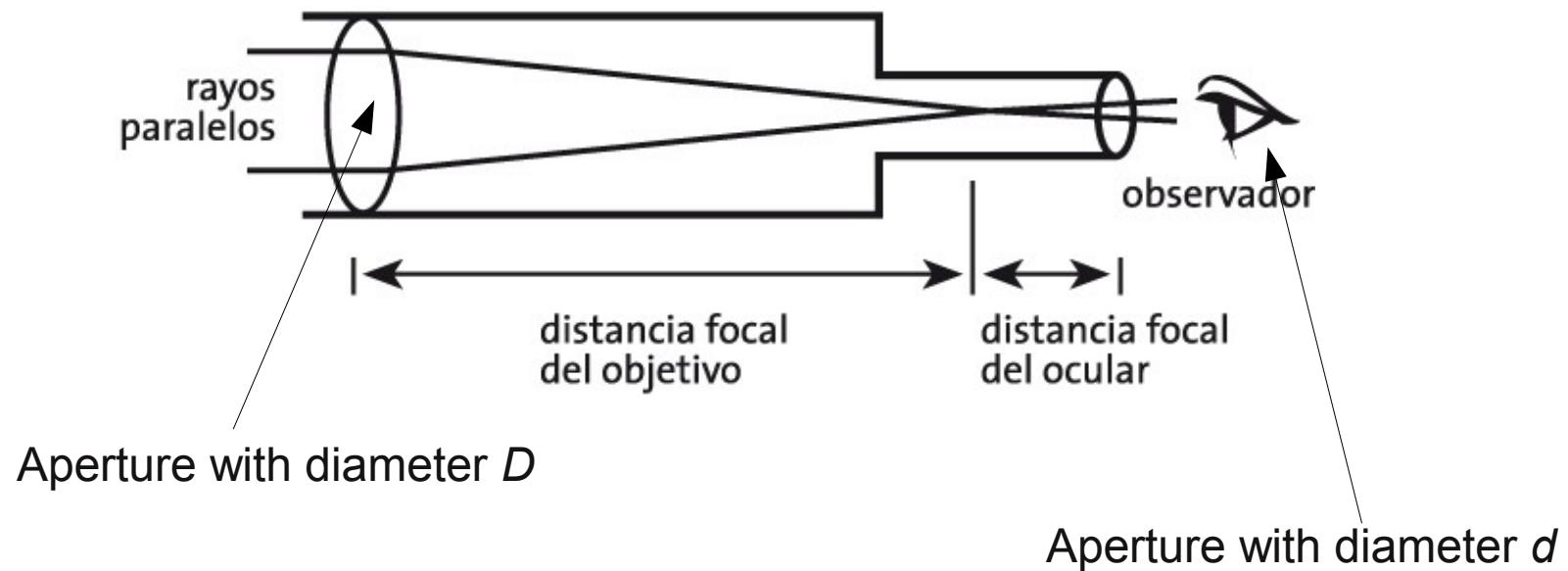
# Observational limitations

## 2) Aperture limit



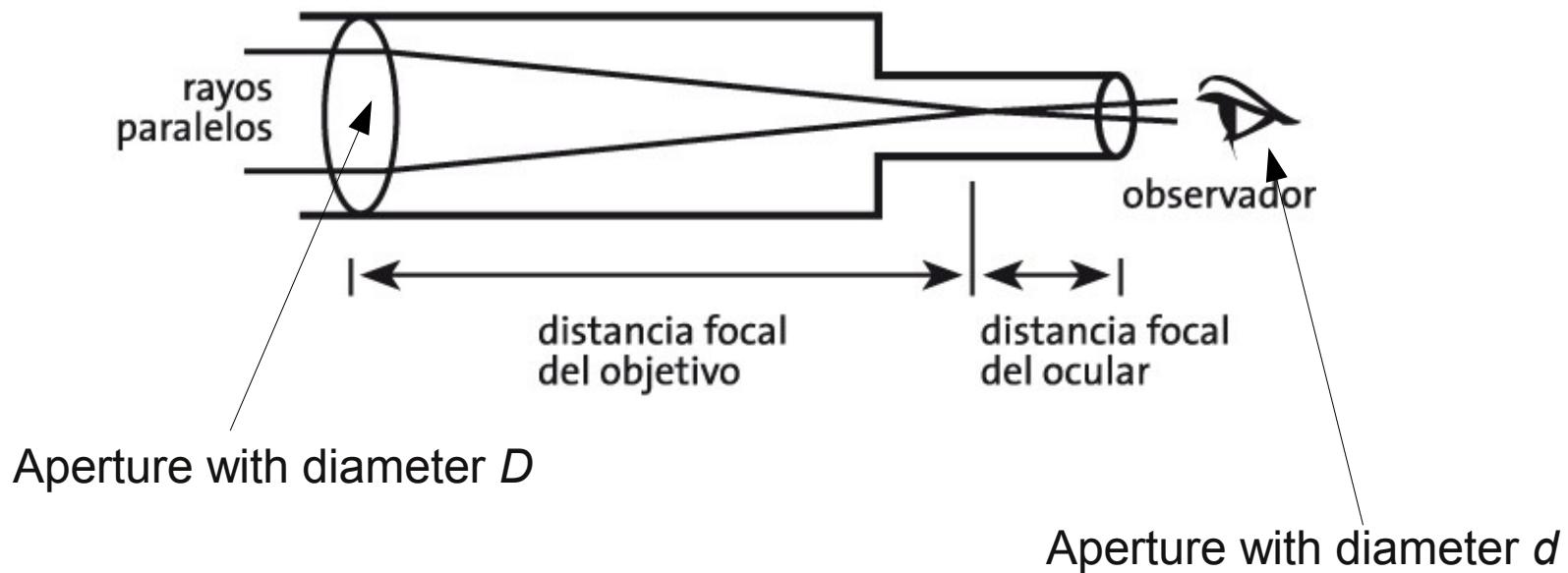
# Observational limitations

## 2) Aperture limit



# Observational limitations

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Flux received by naked eye

$$\frac{f_0}{f_T} = \left(\frac{d}{D}\right)^2$$

Flux received with the help of a telescope

## Observational limitations

2) Aperture limit

$$\frac{F_T}{F_0} = \left(\frac{d}{D}\right)^2$$

Limiting flux received with  
Telescope aid

Limiting flux received by naked eye

## Observational limitations

2) Aperture limit

$$\frac{F_T}{F_0} = \left( \frac{d}{D} \right)^2 \quad \text{Limiting flux}$$

$$m_T - m_0 = -2.5 \log(F_T/F_0) \quad \text{Limiting magnitude}$$

## Observational limitations

2) Aperture limit

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$$m_T - m_0 = -5 \log(d/D)$$

If we set  $m=6$  for the limiting magnitude of the naked eye, the last equation becomes:

$$m_T = m_{lim} = 6 + 5 \log(D/d)$$

## Observational limitations

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If we set  $m=6$  for the limiting magnitude of the naked eye, the last equation becomes:

$$m_T = m_{lim} = 6 + 5 \log(D/d)$$

For  $d=8\text{mm}$  (pupil diameter), this equation reads:

$$m_T = m_{lim} = 16.5 + 5 \log D[m]$$

## Observational limitations

2) Aperture limit

$$m_T = m_{lim} = 16.5 + 5 \log D [m]$$



Could be 16.0 considering inefficiency of the optics

Example 1 telescope amateur, D=0.3m:  $m_{lim} = 13.4$

## Observational limitations

2) Aperture limit

$$m_T = m_{lim} = 16.5 + 5 \log D [m]$$



Could be 16.0 considering inefficiency of the optics

Example 1 telescope amateur, D=0.3m:  $m_{lim} = 13.4$

Example 2 GOTO, D=0.4m:  $m_{lim} = 14.0$

## Observational limitations

### 2) Aperture limit

$$m_T = m_{lim} = 16.5 + 5 \log D [m]$$

This limiting magnitude is constrained by the sampling rate of the human eye. If we now consider an integration factor that is higher by a factor of "f":

$$\frac{fF_T}{F_0} = \left(\frac{d}{D}\right)^2$$

## Observational limitations

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$$m_T = m_{lim} = 16.0 + 5 \log D [m] + 2.5 \log f$$

## Observational limitations

2) Aperture limit

$$m_T = m_{lim} = 16.0 + 5 \log D [m] + 2.5 \log f$$

Assuming a sampling rate of 1/30 s, the above equation becomes:

$$m_T = m_{lim} = 19.7 + 5 \log D [m] + 2.5 \log t [s]$$

## Observational limitations

2) Aperture limit (Simple case)

$$m_T = m_{lim} = 16.0 + 5 \log D [m] + 2.5 \log f$$

Assuming a sampling rate of 1/30 s, the above equation becomes:

$$m_T = m_{lim} = 19.7 + 5 \log D [m] + 2.5 \log t [s]$$

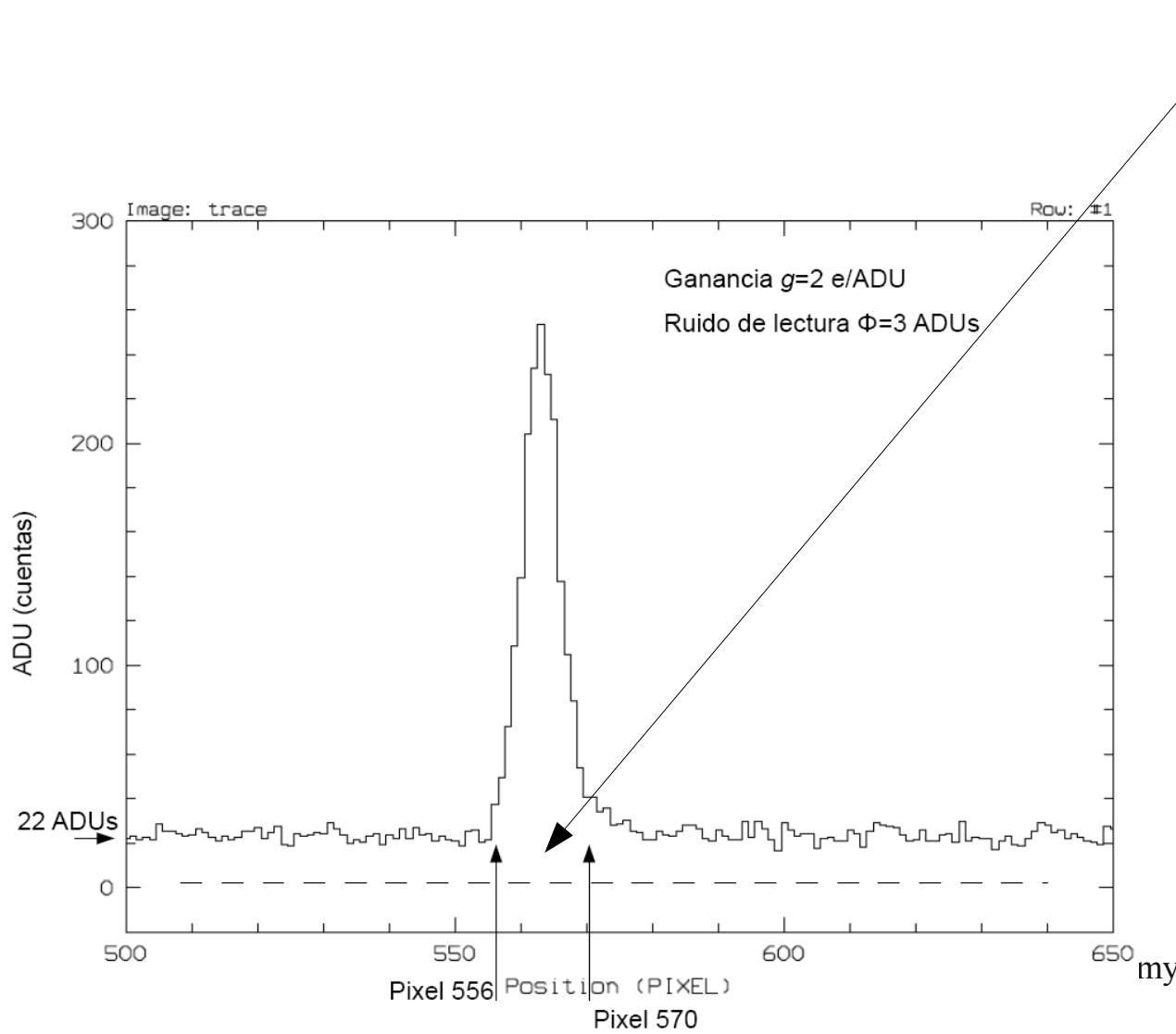
Example: 3.6m telescope at La Silla,  $t= 1800$  s gives  $m=29$ !

However, this limiting magnitude is highly over-estimated. It neglects the effects of the detector noise, the sky background, and the seeing.

# Observational limitations

## 2) Aperture limit (More realistic case)

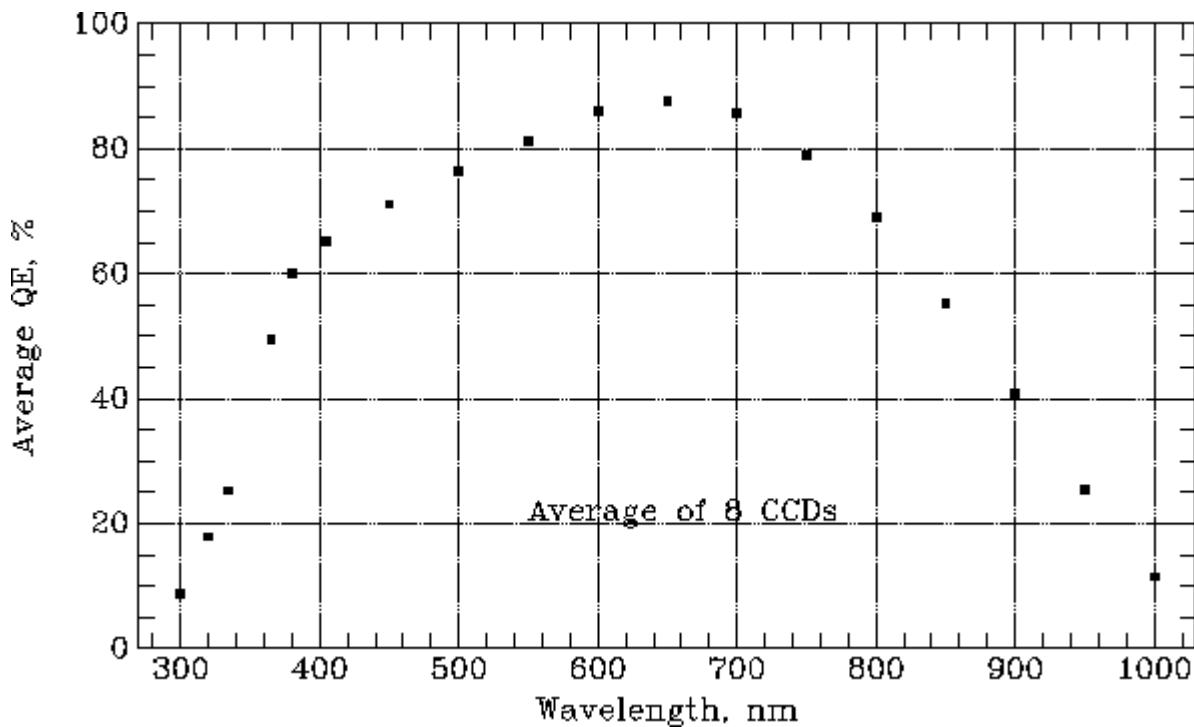
- Aperture has  $m$  pixels



# Observational limitations

## 2) Aperture limit (More realistic case)

- Aperture has  $m$  pixels
- Detector has Quantum Efficiency QE



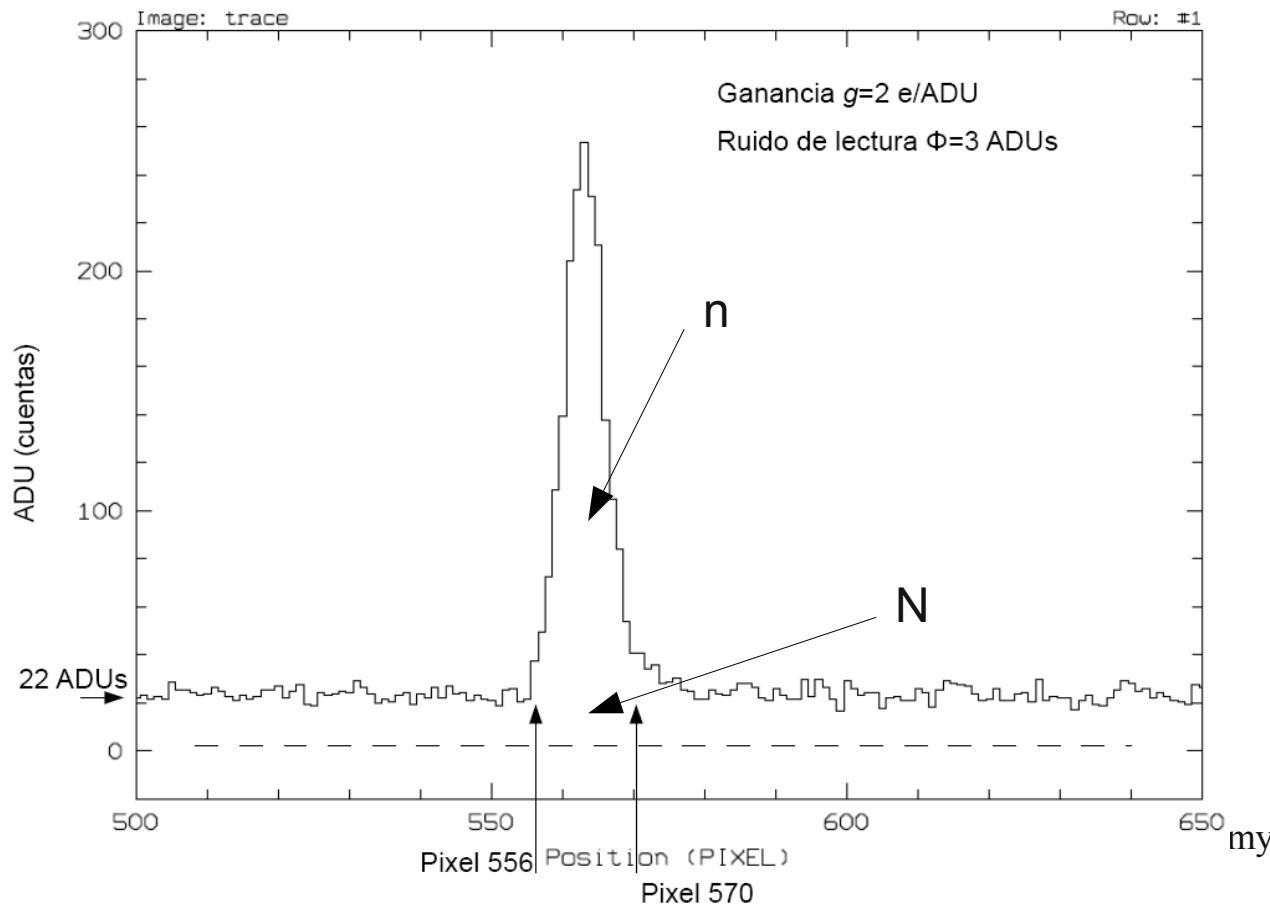
QE: percentage of photons that will produce a photo-electron on the CCD

QE of the red camera of the MIKE spectrograph on Clay @ LCO

# Observational limitations

## 2) Aperture limit (More realistic case)

- Aperture has  $m$  pixels
- Detector has Quantum Efficiency QE
- Read-out noise “ $\Phi$ ”



$$\frac{S}{N} = \frac{nq}{\sqrt{nq + Nq + \Phi^2 m}}$$